Secure Reversible Data Hiding in Encrypted Images by Allocating Memory before Encryption via Security keys

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Abstract—Digital Image and information embedding systems have a number of important multimedia applications. These systems embed one signal, sometimes called an “embedded signal” or “information” within another signal, called as “Host Signal”. In recent times, more and more awareness is paid to reversible data hiding (RDH) in encrypted images. Reason being, it maintains the superlative property that the original cover can be lostlessly recovered after embedded data is extracted while shielding the image content’s privacy. All earlier methods embed data by reversibly vacating room from the encrypted images. However, this may be subject to some slip-up on data extraction and/or image restoration. In this paper, we put forward a narrative method by reserving room before encryption with a conventional RDH algorithm. Hence, it is trouble-free for the data hider to reversibly embed data in the encrypted image. The projected technique can pull off real reversibility, that is, data extraction and image recovery are free of any error. We also develop a framework in which the performance of an information embedding method may be characterized based on its achievable rate-distortion-robustness trade-offs and discuss how previously proposed data hiding algorithms fit into this framework.

Index Terms—Image Encryption, Reversible data hiding, Image and data Recovery.

I. INTRODUCTION

Information embedding and data hiding systems play a key role in addressing couple of major challenges that have arisen from the widespread distribution of multimedia content over digital communication networks. In particular, these systems are enabling technologies for (1) enforcing and protecting copyrights, (2) authenticating and detecting tampering of multimedia signals & images. This significant system is widely used in medical imagery, military imagery and law forensics, where no distortion of the original cover is acceptable. Since first introduced, RDH has attracted considerable research interest.

In theoretical aspect, Kalker and Willems [1] established a rate-distortion model for RDH, through which they proved the rate-distortion bounds of RDH for memory-less covers and proposed a recursive code construction which, however, does not approach the bound. Zhang et al. [2], [3] improved the recursive code construction for binary covers and proved that this construction can achieve the rate-distortion bound as long as the compression algorithm reaches entropy, which establishes the equivalence between data compression and RDH for binary covers.

In practical aspect, many RDH techniques have emerged in recent years. Fridrich et al. [4] constructed a general framework for RDH. By first extracting compressible features of original cover and then compressing them losslessly, spare space can be saved for embedding auxiliary data. A more popular method is based on difference expansion (DE) [5], in which the difference of each pixel group is expanded, e.g., multiplied by 2, and thus the least significant bits (LSBs) of the difference are all-zero and can be used for embedding messages. Another promising strategy for RDH is histogram shift (HS) [6], in which space is saved for data embedding by shifting the bins of histogram of gray values. The state-of-art methods [7]–[11] usually combined DE or HS to residuals of the image, e.g., the predicted errors, to achieve better performance. With regard to providing confidentiality for images, encryption [12] is an effective and popular means as it converts the original and meaningful content to incomprehensible one. In [13], Hwang et al. Advocated a reputation-based trust-management scheme enhanced with data coloring (a way of embedding data into covers) and software watermarking, in which data encryption and coloring offer possibilities for upholding the content owner’s privacy and data integrity.
Obviously, the cloud service provider has no right to introduce permanent distortion during data coloring into encrypted data. Thus, a reversible data coloring technique based on encrypted data is preferred. Suppose a medical image database is stored in a data center, and a server in the data center can embed notations into an encrypted version of a medical image through a RDH technique. With the notations, the server can manage the image or verify its integrity without having the knowledge of the original content, and thus the patient’s privacy is protected. On the other hand, a doctor, having the cryptographic key, can decrypt and restore the image in a reversible manner for the purpose of further diagnosing.

II. WHAT IS RDH (REVERSIBLE DATA HIDING?)

Reversible data hiding is a procedure to embed extra message into some distortion-unacceptable cover media, such as military or medical images, with a reversible behavior so that the original cover content can be flawlessly restored.

In [16], Zhang divided the encrypted image into several blocks. By flipping 3 LSBs of the half of pixels in each block, room can be vacated for the embedded bit. The data extraction and image recovery proceed by finding which part has been flipped in one block. This process can be realized with the help of spatial correlation in decrypted image. Hong et al. [17] ameliorated Zhang’s method at the decoder side by further exploiting the spatial correlation using a different estimation equation and side match technique to achieve much lower error rate. These two methods mentioned above rely on spatial correlation of original image to extract data. That is, the encrypted image should be decrypted first before data extraction. To separate the data extraction from image decryption, Zhang [18] emptied out space for data embedding following the idea of compressing encrypted images [14], [15]. Compression of encrypted data can be formulated as source coding with side information at the decoder [14], in which the typical method is to generate the compressed data in lossless manner by exploiting the syndromes of parity-check matrix of channel codes. The method in [18] compressed the encrypted LSBs to vacate room for additional data by finding syndromes of a parity-check matrix, and the side information used at the receiver side is also the spatial correlation of decrypted images.

All the three methods try to vacate room from the encrypted images directly. However, since the entropy of encrypted images has been maximized, these techniques can only achieve small payloads [16], [17] or generate marked image with poor quality for large payload [18] and all of them are subject to some error rates on data extraction and/or image restoration. Although the methods in [16], [17] can eliminate errors by error correcting codes, the pure payloads will be further consumed. In the present paper, we propose a novel method for RDH in encrypted images, for which we do not “vacate room after encryption” as done in [16]–[18], but “reserve room before encryption”.

III. PROPOSED SCHEME

As we know losslessly vacating rooms from the encrypted images is comparatively intricate and at times unproductive, why are we still so fanatical to discover novel RDH techniques running directly for encrypted images?

Imagine if we reverse the order of encryption and vacating room, i.e., reserving room prior to image encryption at content owner side. The RDH tasks in encrypted images would be more natural and much easier which guide us to the novel framework, “reserving room before encryption (RRBE)”. As shown in Fig. 1(b), the content owner first reserves adequate space on original image. Then translate the image into its encrypted version with the encryption key. Now, the data embedding process in encrypted images is essentially reversible. Data hider only needs to have room for data into the spare space previous emptied out. The data extraction and image recovery are indistinguishable to that of Framework VRAE. Noticeably, standard RDH algorithms are the best operator for reserving room before encryption. This can be effortlessly applied to Framework RRBE to realize better performance compared with techniques from Framework VRAE. Reason is, in this new framework, we pursue the customary idea that first losslessly compresses the unneeded image content (e.g., using excellent RDH techniques) and then encrypts it with respect to protecting privacy.

In the proposed method (Fig 1(b)),

1. We first empty out room by embedding LSBs of some pixels into other pixels with a traditional RDH method.
2. Then encrypt the image, so the positions of these LSBs in the encrypted image can be used to embed data. This proposed method does below:
   1. Separate data extraction from image decryption
   2. Achieves excellent performance in two different prospects:
      a. Real reversibility is realized, that is, data extraction and image recovery are free of any error.
      b. For given embedding rates, the PSNRs of decrypted image containing the embedded data are significantly improved; and for the acceptable PSNR, the range of embedding rates is significantly enlarged.

![Flowchart demonstrating the process of data embedding and extraction.](image)

**A. Image Encryption**

Assuming original color image size is $N1*N2$ and each pixel of Red, green, blue value falling into $[0,255]$ is represented by 8 bits. Denote each bits of a pixel represented as $b_{j,k,0}, b_{j,k,1}, \ldots, b_{j,k,7}$ where $1 \leq j \leq N1$ and $1 \leq k \leq N2$, and the rgb value as $q_{j,k}$. Denote the other number of pixels as $N(N=N1XN2)$.

\[
B_{j,k,a} = \lfloor q_{j,k,a}/2^a \rfloor \mod 2, \quad a=0,1,\ldots,7 \quad (1)
\]

\[
q_{j,k,a} = 2^a \quad (2)
\]

\[
b_{j,k,a} = b_{j,k,a} + r_{j,k,a} \quad (3)
\]

In encryption phase original bits and pseudo-random bits are calculated by exclusive-or. Where $r_{j,k,a}$ are determined by an encryption key using a standard stream cipher.

**B. Data Embedding**

In the data embedding, some parameters $D,H,R$ are embedded into a small number of encrypted pixels, and the other encrypted pixels of LSB are compressed to creating a sparse space for accommodating the additional data. The detailed procedure is as follows. After encrypting the original color image content owner pseudo-randomly
selects \( N_t \) encrypted pixels according to a data hiding key that will be used to carry the parameters \((D,H,R)\) for data hiding. Here, \( N_t \) is a small positive integer. The other \( N-N_t \) encrypted pixels are pseudo-randomly permuted and divided into a number of groups using data hiding key, each group contains no of pixels which is denoted as \( H \). Collect the \( D \) least significant bits of the \( H \) pixels in each group, which is denoted by \( B(g,1), B(g,2), \ldots, B(g,D,H) \) where \( g \) is a group index within \([1,(N-N_t)/H]\) and \( D \) is a positive integer less than 5. Here, \( S \) is a small positive integer.

The content owner generates a \( M \) matrix which has two parts by (4).

\[
M = [ID,H-R \, F] \tag{4}
\]

Where \( ID,H-R \) is an identity matrix \( ID,H-R = (D,H-R) \times (D,H-R) \) and \( F = (D,H-R)XR \) which is derived from the data-hiding key. Then, The parameters \( D,H, \) and \( R \) embedded into the LSB of \( N_t \). For example if \( N_t = 16 \) the values of \( D,H \) and \( R \) are represented as 2, 12 and 2 bits respectively, and \( N_t \) LSB encrypted pixels replaced by 16 bits.

In following, a total bits made up of \( N_t \) and \( (N-N_t)/R \) additional bits will be embedded into the pixel groups. For each group, calculate

\[
B'(g,1) = B'(g,1) \mod 2 \tag{5}
\]

Which is determined by modulo-2.

For data accommodation compress the bits of \( B(g,1), B(g,2), \ldots, B(g,D,H) \) as \((D,H-R)\) bits. In each group, the original LSB of selected encrypted pixels and the additional data to be embedded as \([B'(g,D,H-R+1), B'(g,D,H-R+2), \ldots, B'(g,D,H)]\). Then, replace the new \([B'(g,1), B'(g,2), \ldots, B'(g,D,H)]\), with \( B(g,1), B(g,2), \ldots, B(g,D,H) \) and put into their original positions by reversible manner. At the same time, the most significant bits (MSB) of encrypted pixels are kept unchanged. Since bits are embedded into each pixel-group, the total \((N-N_t)/R\) bits can be accommodated in all groups. Figure 3 shows the original input image and figure 4 shows the result of encrypted image containing embedded data.

### C. Data Extraction and Image Recover

In this phase, there are three options at the receiver side:

- **a)** If the receiver has only data hiding key, receiver can extract the data and does not know about the original content.
- **b)** If the receiver has only encryption key, receiver can decrypt the image and does not know about the hidden data.
c) If the receiver has both encryption and data hiding key, receiver can extract the data and also recover the original content.

(a) In first option, with an encrypted image containing embedded data, receiver may first obtain the values of the parameters D, H and R from the LSB of the Nt selected encrypted pixels. Then, the receiver permutes and divides the other (N-Nt) pixels into (N-Nt)/R groups and extracts the R embedded bits from the D LSB-planes of each group. When having the total (N-Nt)R/H extracted bits, the receiver can divide them into Nt original LSB of selected encrypted pixels and (N-Nt)R/H-Nt additional bits. Note that because of the pseudo-random pixel selection and permutation, any attacker without the data-hiding key cannot obtain the parameter values and the pixel-groups, therefore cannot extract the embedded data. Furthermore, if the receiver having the data-hiding key can successfully extract the embedded data, receiver cannot get any information about the original image content.

(b) In second option, if the receiver has the encryption key but does not know the data-hiding key. Clearly, receiver cannot obtain the parameter values therefore cannot extract the embedded data. However, the original image content can be roughly recovered using encryption key. Denoting the bits of pixels in the encrypted image containing embedded data as B'j,k,0, B'j,k,1........ B'j,k,7 the receiver can decrypt the data

\[ b'_{j,k} = b_{j,k,0} + r_{j,k} \]  \hspace{1cm} (6)

The rgb values of decrypted pixels are

\[ P_{j,k} = \sum_{i=0}^{2^a} b_{j,k,a} 2^a \]  \hspace{1cm} (7)

Figure 5 shows the result of directly decrypted image using decryption key.

The decrypted MSB must be same as the original MSB. Since the data-embedding operation does not alter any MSB of encrypted image. So, the content of decrypted image is similar to that of original image. If B(g,D,H-R+1)=B(g,D,H-R+2)=......=B(g,D,H-R)=0 there is B'(g,x)=B(g,x), x=1,2,......D,H-R, (8) The probability of this case is 1/2R and the original bits in D LSB-planes can be decrypted correctly. Since R is significantly less than D.H.
Here, the distortion in the selected pixels Nt is also ignored since their number is significantly less than the image size. So, the value of PSNR in the directly decrypted image is

$$\text{PSNR} = 10 \log_{10}(A_E).$$

In third option, If the receiver has both the data-hiding and the encryption keys, receiver may aim to extract the embedded data and recover the original content. According to the data-hiding key, the values of D,H and R, and the (N-Nt)R/H-Nt additional bits can be extracted from the encrypted image containing embedded data. By putting the Nt LSB into their original positions, the encrypted data of the Nt selected pixels are retrieved, and their original rgb values can be correctly decrypted using the encryption keys. In the following, we will recover the original rgb values of the other pixels. Figure 6 shows the result of decrypted image after extracting the hidden data which is similar to original image.

Where the estimated rgb values are generated from the neighbors in the directly decrypted image Clearly, the estimated rgb values are only dependent on the MSB of neighbour pixels. Thus, let have 2R different Di corresponding to the 2R decrypted pixel-group Fg. Among the 2R decrypted pixel-group, there must be one that is just the original rgb values and possesses a low Di because of the spatial correlation in natural image. To keep a low computation complexity, let R be less than ten and use only the four neighboring pixels to calculate the estimated values.

**IV. CONCLUSION**

Reversible data hiding in encrypted images is a new topic which is attracting more interest because of the privacy-preserving requirements from cloud data management. Earlier methods implement RDH in encrypted images by vacating room after encryption, as opposed to which we proposed by reserving room before encryption. In new method data hider can benefit from the extra space emptied out in previous stage to make data hiding process effortless. The proposed method can take:

1. Assistance of all traditional RDH techniques for plain images.
2. Achieve excellent performance without loss of perfect secrecy.
3. Furthermore, this novel method can achieve real reversibility, separate data extraction and greatly improvement on the quality of marked decrypted images.

**REFERENCES**


